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Smoothing PLLs for QAM Dynamical Phase Estimation

J. Yang, B. Geller, C. Herzet, and J.M. Brossier¹

Abstract—This paper presents a near-optimum, low-complexity, fixed-interval smoothing algorithm that approaches the performance of an optimal smoother for the price of two low-complexity sequential estimators (two PLLs). The proposed Smoothing PLL (S-PLL) algorithm is easy to implement and fits the Cramer-Rao bounds over a wide range of signal-to-noise ratios. Moreover we show that, compared to the conventional forward loop, the proposed scheme allows to have a large gain of several dBs and is able to track frequency offsets.

Keywords—Dynamical Phase Estimation; Phase-Locked Loop (PLL); QAM; Smoothing Algorithm.

I. INTRODUCTION

Due to the increasing requirements of modern communication systems to face the physical channel (low signal-to-noise ratio, high data rates), phase estimation is more challenging than ever before. Since phase errors rapidly degrade the overall performance of communication systems, synchronization has recently become one of the most challenging tasks that a digital receiver has to cope with.

Noels et al [1],[2] derived a maximum likelihood (ML) algorithm for the problem of constant phase estimation, and then applied a first-order and a second order phase-locked loop (PLL) based algorithm for the coded BPSK and QPSK dynamical phase estimation. The corresponding performances are limited both by the on-line bound and by a non-zero phase MSE floor. On the contrary, this paper deals with the non data aided (NDA) estimation of a time-varying phase and proposes an off-line Smoothing PLL (S-PLL) algorithm. To assess the performance of such algorithms, Bayesian and hybrid Cramér-Rao Bounds (BCRB and HCRB) associated to this dynamical phase synchronization problem have already been considered in some recent contributions [3]-[6] and clearly show the superiority of the off-line scenario [7].

In practice, on-line estimators are often considered for complexity considerations. Among the famous algorithms, phase-locked loops are recognized low-cost devices for on-line estimation and have been integrated in many existing systems [8]-[11]. Despite a poor transient behaviour, their excellent asymptotic (i.e. tracking) characteristic makes them a reference from the performance-complexity trade-off point of view. The

poor transient behaviour has now been handled by several authors for many years (see e.g. [12]). The good performance of such PLLs can even be improved at low SNRs within the turbo-receiver framework (see e.g. [1],[2],[13]) but this paper is definitely not concerned about the code-aided framework. [14] proposed a CA belief-propagation (BP) algorithm for the BPSK dynamical phase estimation but the computation complexity of the proposed BP algorithm is rather high. This paper is concerned with a very simple synchronizing scheme for any QAM modulated signal which is able to operate near the off-line time-varying phase bounds. To our knowledge, it was first proposed without any justification and without any performance evaluation in [15]-[17]; contrarily to [1],[2], it takes advantage of averaging two phase trajectories provided by two PLLs, so that this S-PLL algorithm is able to have such a near off-line Cramér-Rao bound performance.

The rest of the paper is organized as follows. In section II, we give the system model. In section III, we derive from the MAP estimation theory the proposed algorithm where the smoothing effect is achieved through two PLLs working in opposite time directions. Finally in section IV, we present the simulation results before giving some conclusions.

II. SYSTEM MODEL

We consider the transmission of a complex-valued QAM modulated sequence $\mathbf{c} = [c_1, \dots, c_K]^T$ ($c_k \in \mathbf{S}_M$) over an AWGN channel affected by some carrier phase offsets stacked in a vector $\boldsymbol{\theta} = [\theta_1, \dots, \theta_K]^T$. Assuming that the timing recovery is perfect without any inter-symbol interference (ISI), the sampled baseband signal $\mathbf{y} = [y_1, \dots, y_K]^T$ is written as:

$$y_k = c_k e^{j\theta_k} + n_k, \quad (1)$$

where c_k , θ_k and n_k are respectively the i.i.d. k -th unknown transmitted constellation symbol ($p(c_k) = 1/M$), the residual phase distortion and the zero mean complex-valued circular Gaussian noise with known variance σ_n^2 . We suppose that the system operates in a non-data aided (NDA) mode. Hence, the conditional probability based on the known phase θ_k is:

$$p(y_k | \theta_k) = \sum_{c_k} p(y_k | \theta_k, c_k) p(c_k) = \frac{1}{M \pi \sigma_n^2} \exp \left\{ -\frac{|y_k|^2}{\sigma_n^2} \right\} \sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k), \quad (2)$$

$$\text{where } \Omega(c_k, y_k, \theta_k) = \exp \left\{ \frac{-|c_k|^2 + 2 \operatorname{Re} \{ y_k c_k^* e^{-j\theta_k} \}}{\sigma_n^2} \right\}.$$

In practice, due to the rapid variant channel and the imperfections of the functional blocks before the phase

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estimation, the residual phase distortion can be modeled efficiently by a Brownian motion. The corresponding phase model is:

$$\theta_k = \theta_{k-1} + \xi + w_k, \quad (3)$$

where θ_k is the unknown phase offset at time k , ξ is the unknown constant frequency offset (linear drift), w_k is a real-valued white Gaussian noise with zero mean and variance σ_w^2 . This model is commonly used [18]-[21] in order to describe the behavior of practical oscillators for which the frequency is randomly perturbed. Based on (3), the corresponding conditional probability can be expressed as:

$$p(\theta_k | \theta_{k-1}, \xi) = \frac{1}{\sqrt{2\pi}\sigma_w} \exp\left\{-\frac{(\theta_k - \theta_{k-1} - \xi)^2}{2\sigma_w^2}\right\}. \quad (4)$$

III. RATIONALE FOR A FORWARD / BACKWARD APPROACH BY MAP ESTIMATION THEORY

In the MAP estimation approach, one classically chooses $\hat{\theta}$ to maximize the posterior pdf [22]:

$$\hat{\theta} = \arg \max_{\theta} p(\theta | \mathbf{y}) = \arg \max_{\theta} [\ln p(\mathbf{y} | \theta) + \ln p(\theta)] \quad (5)$$

Based on the model described by (2) and (4), the joint pdf of the observations and the parameters can be written as:

$$\begin{aligned} p(\mathbf{y}, \theta, \xi) &= p(\mathbf{y} | \theta) p(\theta | \xi) \\ &= p(\theta_1) p(y_1 | \theta_1) \prod_{k=2}^K p(y_k | \theta_k) p(\theta_k | \theta_{k-1}, \xi) \\ &= \left(\frac{1}{M\pi\sigma_n^2}\right)^K \left(\frac{1}{\sqrt{2\pi}\sigma_w}\right)^{K-1} p(\theta_1) \exp\left\{-\frac{|y_1|^2}{\sigma_n^2}\right\} \left(\sum_{c_1 \in \mathbf{S}_M} \Omega(c_1, y_1, \theta_1)\right) \\ &\quad \cdot \prod_{k=2}^K \exp\left\{-\frac{|y_k|^2}{\sigma_n^2} - \frac{(\theta_k - \theta_{k-1} - \xi)^2}{2\sigma_w^2}\right\} \left(\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)\right) \end{aligned} \quad (6)$$

It is easy to obtain for any θ_k the first derivative of $\ln[p(\mathbf{y}, \theta, \xi)]$:

$$\frac{\partial \ln[p(\mathbf{y}, \theta, \xi)]}{\partial \theta_1} = \frac{\partial \ln[p(\theta_1)]}{\partial \theta_1} + \frac{\sum_{c_1 \in \mathbf{S}_M} \frac{\partial \Omega(c_1, y_1, \theta_1)}{\partial \theta_1}}{\sum_{c_1 \in \mathbf{S}_M} \Omega(c_1, y_1, \theta_1)} + \frac{(\theta_2 - \theta_1 - \xi)}{\sigma_w^2},$$

$$\frac{\partial \ln[p(\mathbf{y}, \theta, \xi)]}{\partial \theta_k} = \frac{\sum_{c_k \in \mathbf{S}_M} \frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k}}{\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)} - \frac{(2\theta_k - \theta_{k-1} - \theta_{k+1})}{\sigma_w^2}$$

for $2 \leq k \leq K-1$,

$$\frac{\partial \ln[p(\mathbf{y}, \theta, \xi)]}{\partial \theta_K} = \frac{\sum_{c_K \in \mathbf{S}_M} \frac{\partial \Omega(c_K, y_K, \theta_K)}{\partial \theta_K}}{\sum_{c_K \in \mathbf{S}_M} \Omega(c_K, y_K, \theta_K)} - \frac{(\theta_K - \theta_{K-1} - \xi)}{\sigma_w^2}. \quad (7)$$

where $\frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k} = \Omega(c_k, y_k, \theta_k) \frac{2}{\sigma_n^2} \text{Im}\{y_k c_k^* e^{-j\theta_k}\}$. Looking for the MAP estimator implies that one must set the first derivative $\frac{\partial \ln[p(\mathbf{y}, \theta, \xi)]}{\partial \theta_k}$ equal to 0, so that:

$$\begin{aligned} \theta_1 &= \theta_2 - \xi + \sigma_w^2 \frac{\sum_{c_1 \in \mathbf{S}_M} \frac{\partial \Omega(c_1, y_1, \theta_1)}{\partial \theta_1}}{\sum_{c_1 \in \mathbf{S}_M} \Omega(c_1, y_1, \theta_1)} + \sigma_w^2 \frac{\partial \ln[p(\theta_1)]}{\partial \theta_1}, \\ \theta_k &= \frac{1}{2} \left[\left(\theta_{k-1} + \frac{\sigma_w^2}{2} \frac{\sum_{c_k \in \mathbf{S}_M} \frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k}}{\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)} \right) + \left(\theta_{k+1} + \frac{\sigma_w^2}{2} \frac{\sum_{c_k \in \mathbf{S}_M} \frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k}}{\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)} \right) \right] \end{aligned}$$

for $2 \leq k \leq K-1$,

$$\theta_K = \theta_{K-1} + \sigma_w^2 \frac{\sum_{c_K \in \mathbf{S}_M} \frac{\partial \Omega(c_K, y_K, \theta_K)}{\partial \theta_K}}{\sum_{c_K \in \mathbf{S}_M} \Omega(c_K, y_K, \theta_K)} + \xi. \quad (8)$$

Rewrite $\frac{\sum_{c_k \in \mathbf{S}_M} \frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k}}{\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)}$ as below in order to get the physical meaning of the term:

$$\begin{aligned} \frac{\sum_{c_k \in \mathbf{S}_M} \frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k}}{\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)} &= \frac{\sum_{c_k \in \mathbf{S}_M} \exp\left\{-\frac{|c_k|^2}{\sigma_n^2} + 2\text{Re}\{y_k c_k^* e^{-j\theta_k}\}\right\} \frac{2\text{Im}\{y_k c_k^* e^{-j\theta_k}\}}{\sigma_n^2}}{\sum_{c_k \in \mathbf{S}_M} \exp\left\{-\frac{|c_k|^2}{\sigma_n^2} + 2\text{Re}\{y_k c_k^* e^{-j\theta_k}\}\right\}} \\ &= \frac{2}{\sigma_n^2} \sum_{c_k \in \mathbf{S}_M} \frac{p(y_k | c_k, \theta_k)}{\sum_{\tilde{c}_k \in \mathbf{S}_M} p(y_k | \tilde{c}_k, \theta_k)} \text{Im}\{y_k c_k^* e^{-j\theta_k}\}. \end{aligned} \quad (9)$$

One can then recognize that the factor $\text{Im}\{y_k c_k^* e^{-j\theta_k}\}$ is just the classical hard decision phase detector output based on the decision c_k , while the factor $\frac{p(y_k | c_k, \theta_k)}{\sum_{\tilde{c}_k \in \mathbf{S}_M} p(y_k | \tilde{c}_k, \theta_k)}$ is exactly the *a posteriori* probability (APP) $\text{Pr}(c_k | y_k, \theta_k)$ in the NDA scenario.

Thus the term $\frac{\sum_{c_k \in \mathbf{S}_M} \frac{\partial \Omega(c_k, y_k, \theta_k)}{\partial \theta_k}}{\sum_{c_k \in \mathbf{S}_M} \Omega(c_k, y_k, \theta_k)}$ can be interpreted as the soft decision phase detector output. (9) can then be written as:

$$\begin{cases} \theta_1 = \theta_2 - \xi + \frac{2\sigma_w^2}{\sigma_n^2} \sum_{c_1 \in \mathbf{S}_M} \text{Pr}(c_1 | y_1, \theta_1) \text{Im}\{y_1 c_1^* e^{-j\theta_1}\} + \sigma_w^2 \frac{\partial \ln[p(\theta_1)]}{\partial \theta_1}, \\ \theta_k = \frac{1}{2} (\theta_k^{(F)} + \theta_k^{(B)}) & \text{for } 2 \leq k \leq K-1, \\ \theta_K = \theta_{K-1} + \frac{2\sigma_w^2}{\sigma_n^2} \sum_{c_K \in \mathbf{S}_M} \text{Pr}(c_K | y_K, \theta_K) \text{Im}\{y_K c_K^* e^{-j\theta_K}\} + \xi, \end{cases} \quad (10)$$

$$\text{where } \begin{cases} \theta_k^{(F)} \square \theta_{k-1} + \frac{\sigma_w^2}{\sigma_n^2} \sum_{c_i \in \mathcal{S}_M} \Pr(c_k | y_k, \theta_k) \text{Im} \{ y_k c_k^* e^{-j\theta_k} \}, \\ \theta_k^{(B)} \square \theta_{k+1} + \frac{\sigma_w^2}{\sigma_n^2} \sum_{c_i \in \mathcal{S}_M} \Pr(c_k | y_k, \theta_k) \text{Im} \{ y_k c_k^* e^{-j\theta_k} \}. \end{cases} \quad (11)$$

Furthermore in (11), $\theta_k^{(F)}$ and $\theta_k^{(B)}$ can be regarded as soft-decision based first-order PLL outputs which are respectively updated in the increasing (Forward) and decreasing (Backward) time directions. The physical meaning of (9) can thus be summarized as following; assuming that we do not have any *a priori* information about the initial phase θ_1 (*i.e.*

$\frac{\partial \ln [p(\theta_1)]}{\partial \theta_1} = 0$), the estimator is just estimated from θ_2 with a

backward recursion PLL; for the last position $k = K$ element, the estimator is estimated from θ_{K-1} with a forward PLL; and in the general case ($1 < k < K$), the phase estimator is estimated both from the previous and the following samples, *i.e.* as the average of a forward and of a backward PLL. Since in practice it is impossible to get the actual phase value θ_k before estimating it, we replace in (11) the true phase θ_k by the forward estimate $\hat{\theta}_{k-1}^{(F)}$ and the backward estimate $\hat{\theta}_{k+1}^{(B)}$:

$$\begin{cases} \hat{\theta}_k^{(F)} \square \hat{\theta}_{k-1}^{(F)} + \frac{\sigma_w^2}{\sigma_n^2} \sum_{c_i \in \mathcal{S}_M} \Pr(c_k | y_k, \hat{\theta}_{k-1}^{(F)}) \text{Im} \{ y_k c_k^* e^{-j\hat{\theta}_{k-1}^{(F)}} \}, \\ \hat{\theta}_k^{(B)} \square \hat{\theta}_{k+1}^{(B)} + \frac{\sigma_w^2}{\sigma_n^2} \sum_{c_i \in \mathcal{S}_M} \Pr(c_k | y_k, \hat{\theta}_{k+1}^{(B)}) \text{Im} \{ y_k c_k^* e^{-j\hat{\theta}_{k+1}^{(B)}} \}. \end{cases} \quad (12)$$

From (8) the “Forward / Backward” (F/B) estimator can thus be written as:

$$\begin{cases} \hat{\theta}_1^{(F/B)} = \hat{\theta}_2^{(B)} - \hat{\xi} + \frac{2\sigma_w^2}{\sigma_n^2} \sum_{c_i \in \mathcal{S}_M} \Pr(c_1 | y_1, \hat{\theta}_2^{(B)}) \text{Im} \{ y_1 c_1^* e^{-j\hat{\theta}_2^{(B)}} \}, \\ \hat{\theta}_k^{(F/B)} = \frac{1}{2} (\hat{\theta}_k^{(F)} + \hat{\theta}_k^{(B)}) \quad \text{for } 2 \leq k \leq K-1, \\ \hat{\theta}_K^{(F/B)} = \hat{\theta}_{K-1}^{(F)} + \hat{\xi} + \frac{2\sigma_w^2}{\sigma_n^2} \sum_{c_i \in \mathcal{S}_M} \Pr(c_K | y_K, \hat{\theta}_{K-1}^{(F)}) \text{Im} \{ y_K c_K^* e^{-j\hat{\theta}_{K-1}^{(F)}} \}. \end{cases} \quad (13)$$

Note that this structure is similar to that of the Kalman smoother valid for linear Gaussian problems. The name “Forward / Backward” stems from the fact that the off-line phase estimation is just the average of a classical (Forward) phase-locked loop and of a Backward phase-locked loop working in the reverse time direction and that can be initialized at the end of the forward PLL. This process can then be iterated, *i.e.* the estimation error at the end of the previous backward loop can be further used as the estimation error at the beginning of the next forward recursion, and several forward and backward recursions can sequentially be proceeded. We call this process in the sequel as “multiple forward / backward”. Restricted by the paper size, we shall give further analysis of the proposed algorithm at the oral presentation.

IV. SIMULATION AND DISCUSSION

In a practical system, a frame header can be used and one could take advantage of it to get rid of the phase ambiguities. In our simulations, we thus assume that the phase ambiguity problem is solved. We evaluate the MSEs in the centre position of the block after 3 F/B iterations over 10^5 Monte-Carlo trials. The block length K for BPSK and QPSK is 60, and is 800 for the 16QAM constellation. We use the following notations in the figures of the present paragraph. “Forward (Sim)” means that the simulation MSE is measured after one (on-line) forward estimation without any backward estimation. The “Forward / Backward (Sim)” means that the MSE of the F/B estimation is measured after three (off-line) F/B iterations.

A. Performance with no linear drift

Since all the parameters are random, we compare the estimation MSE of the “Forward (Sim)” (resp. “Forward / Backward” (Sim)) with the on-line BCRB (resp. the off-line BCRB) [3],[5],[6], on Fig. 1 to Fig. 3 for different constellations.

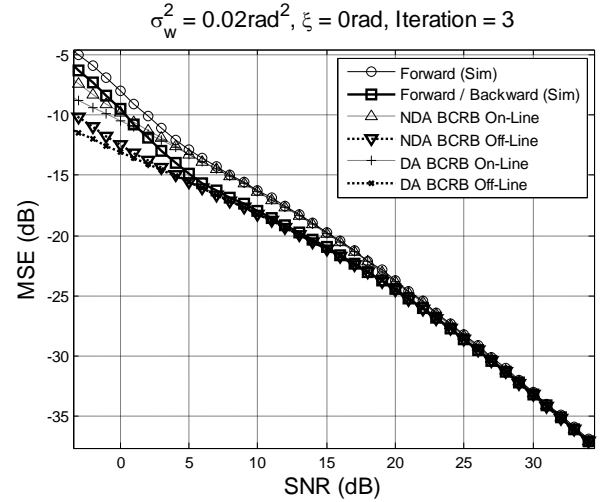


Fig. 1 BPSK MSEs and BCRBs versus SNR

At high SNR, we notice that the forward MSE and the F/B MSE curves logically merge. In this case the observations are reliable enough to only take into account the present observation y_k in order to estimate θ_k ; this is why the off-line BCRBs (corresponding to the F/B MSE) converge to the on-line BCRBs (corresponding to the forward MSE), and this is also why the NDA bounds converge to the DA bounds. As the *a priori* distribution of θ then has very little influence, the Bayesian problem tends to a deterministic phase estimation problem where we estimate independent observations.

In more realistic mid-range SNRs, the F/B performance is definitely superior to the forward only recursion and the maximum difference is 3dB. In this range of SNRs, the *a priori* knowledge on θ plays a very important role in the phase estimation and this is why there is a larger difference

between the F/B and forward recursions compared to higher and lower SNR range.

Finally, at low SNRs, because of the decision error, the MSE increases rapidly and the non-data-aided (NDA) BCRBs do not coincide anymore with the DA BCRBs. However, generally, the performance gain using a data-aided scenario is relatively low compared to the performance difference between the off-line and the on-line scenarios, and logically, when comparing with the forward recursion, there is still an appreciable gain in favor of the F/B recursion.

$$\sigma_w^2 = 0.005\text{rad}^2, \xi = 0\text{rad}, \text{Iteration} = 3$$

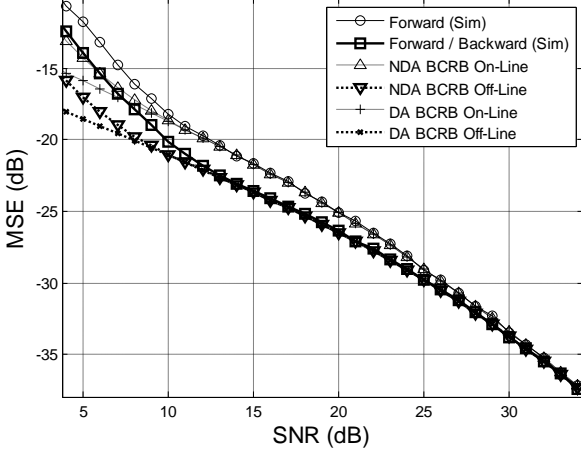


Fig. 2 QPSK MSEs and BCRBs versus SNR

$$\sigma_w^2 = 0.00015\text{rad}^2, \xi = 0\text{rad}, \text{Iteration} = 3$$

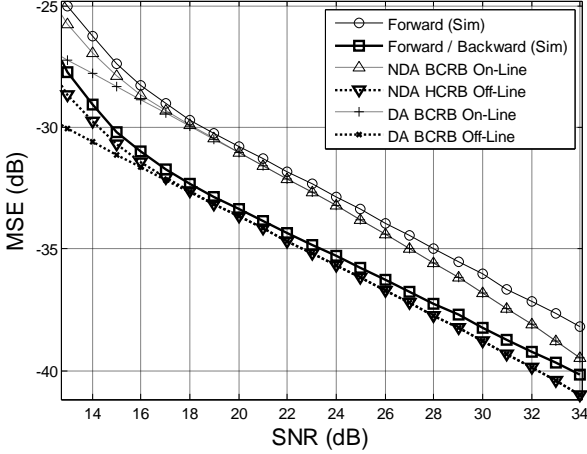


Fig. 3 16QAM MSEs and BCRBs versus SNR

B. Performance with a linear drift

Since the parameters contain both some random parameters θ_k and a deterministic linear drift ξ , we compare the MSEs to HCRBs of interest [4]-[6] for different constellations on Fig. 4 to Fig. 6.

At high SNR, the off-line HCRB coincides with the on-line HCRB, and so are the corresponding MSEs. Because in this range of SNR, the information provided by the observation is

dominating over the *a priori* knowledge on θ , the observation y_k is self-sufficient to estimate θ_k and the error on ξ does not disturb the estimation performance on θ_k .

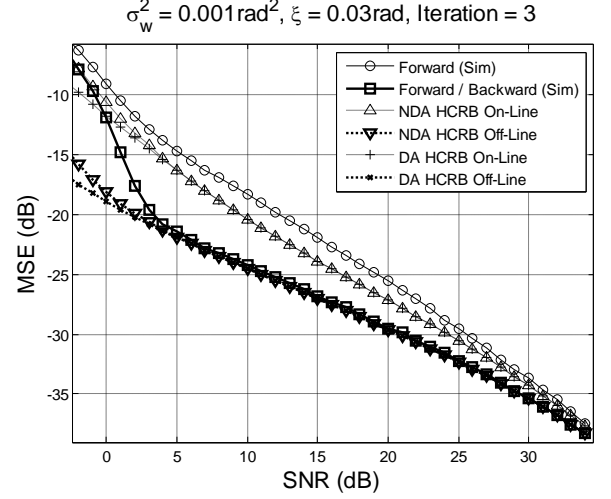


Fig. 4 BPSK MSEs and HCRBs versus SNR

$$\sigma_w^2 = 0.0005\text{rad}^2, \xi = 0.02\text{rad}, \text{Iteration} = 3$$

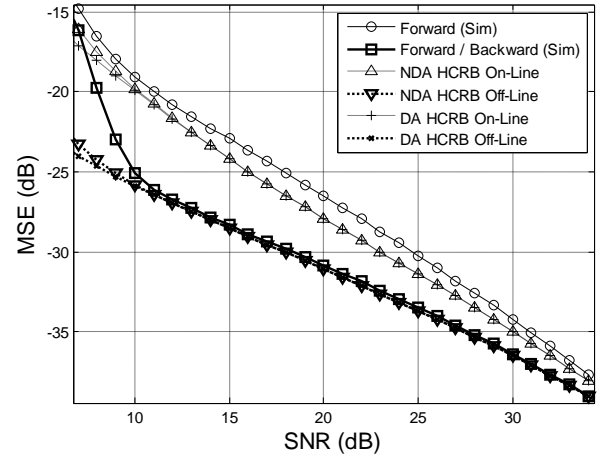


Fig. 5 QPSK MSEs and HCRBs versus SNR

At mid-range SNRs, there is not enough information provided by y_k to estimate the phase and one can take advantage of the *a priori* knowledge on θ (see the difference between the on-line and the off-line BCRBs). The F/B estimation is definitely superior (up to 5 dB on Fig. 4) to the forward MSE not only thanks to the *a priori* knowledge on θ ; this superiority also comes from the fact that the F/B scheme remains unbiased contrarily to the forward 1st order loop which suffers from the high linear drift as the corresponding MSE does not coincide anymore with the on-line HCRB.

At low SNRs, there is still an advantage for the F/B recursion; however the F/B performance of Fig. 4 deteriorates rapidly, because in practice the F/B recursion is made out of two unidirectional loops, and these loops are not able to operate

anymore as wanted with the considered large linear drift. This phenomenon is attenuated with a smaller linear drift (see Fig. 6) or if we had replaced our simple first order PLL components by other component loops such as second order PLLs.

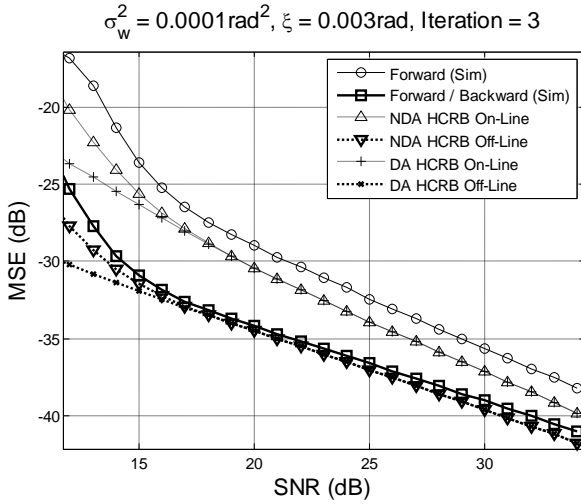


Fig. 6 16QAM MSEs and HCRBs versus SNR

C. Algorithm complexity analysis

The classical on-line PLL has a very low gradient-like complexity and has been employed in real systems for several decades. The complexity price for the off-line improvement is only two times that of the on-line algorithm as we combine two elementary PLLs. In addition, three forward-backward needs to be proceeded which both involves a very reasonable delay and the memorization of K symbols and of $2K$ phase values.

V. CONCLUSION

In this paper, we presented a near-optimum smoothing phase locked loop (S-PLL) algorithm made out of two very simple first order PLLs. The performance of the S-PLL algorithm does not suffer from the poor transient behavior even with a small number of observations. The proposed scheme provides a gain of several dBs over a forward only on-line algorithm and its performance is near the Cramer-Rao bounds of interest. Finally it is very easy to implement and should be very useful in practice.

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